

MA 110-91 §1.1 - 3.1	<b>Test #1</b>	score	Name: _____ 30 September 2000
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1. Use a properly labeled Venn diagram to determine the validity of the following argument.

Explain. (9 points)

1. All nurses are caring.
2. Jill is caring.

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Therefore Jill is a nurse.

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2. Convert the following argument into symbolic form and determine if the argument is valid using a truth table. (10 points)

If math is interesting, then I'll get an A. If I study well, then I'll get an A. I get an A. Therefore, I studied well or math is interesting.

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3. Write the contrapositive of the statement "If I get an A or a B then I will be happy." (8 points)

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4. If  $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14\}$ ,  $A = \{1, 3, 5, 7, 9\}$  and  $B = \{1, 2, 3, 4, 5, 6\}$ , find the set  $A \cap B$ ; then find  $(A' \cup B)'$ . (9 points)

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5. How many subsets are there of a set having 8 elements? Explain how the answer is related to the number of ways a hamburger can be served if there are 8 different condiments for the customer to choose from. (9 points)

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6. In a dorm holding 1000 students, 500 are taking math, 300 are taking biology, and 200 are taking a foreign language. Suppose 25 are taking all three, 75 are taking math and biology, 50 are taking only a foreign language, and 65 are taking math and a foreign language. What percentage of students in the dorm are taking at least one of these three subjects?

Draw and label a Venn diagram and explain your reasoning. (10 points)

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7. Compute the numbers  ${}_8P_5$  and  ${}_8C_5$ . Explain these numbers would be used in a counting argument. (9 points)

8. In how many ways can teams in a 10-team league finish first, second, and third (assuming no ties). Explain your counting argument. (9 points)

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9. From a group of 7 men and 8 women, how many different ways are there to choose a 5-person committee consisting of 3 women and 2 men? Explain your counting argument. (9 points)

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10. How many different 5-card poker hands are a flush (i.e., all cards in the same suit)? (9 points)

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11. What is the probability of rolling a total of 8 on two rolls of a die? Explain your reasoning. (9 points)