

MA 238-01  
§1.9-2.1

## Quiz #3

score

Name: \_\_\_\_\_

29 September 1999

1. Show that the following differential equation is homogeneous and find the general solution. (7 points)

$$\frac{dy}{dx} = \frac{xy + y^2}{x^2}$$

- 
2. A boat travels along a straight line (neglecting the Earth's curvature). To coordinate, suppose the boat starts at the point  $(0,0)$  and travels along the positive  $y$ -axis. At the moment the boat is at the origin, a Coast Guard boat begins pursuing it beginning at the point  $(a,0)$ . The Coast Guard boat always maintains a discrete distance of  $a$  from the original boat. Write a differential equation with initial condition that describes the location of the Coast Guard boat. NOTE: You do not need to solve the IVP. (6 points)

- 
3. Use the method of Picard iterates to find approximate solutions to the initial value problem

$$y' = 2t(y + 1), \quad y(0) = 0$$

You should compute the Picard iterates  $y_0, y_1, y_2,$  and  $y_3$ . (7 points)